

## Free Fall

### Conceptual Questions

1. If an object is accelerating, the velocity of the object (**CHANGES**, ~~STAYS THE SAME~~)
2. An object is thrown upwards. The velocity of the object at its highest point is **ZERO**.
3. If the object had a zero velocity, would the object be moving? (~~YES~~, **NO**)
4. A ball is thrown straight up in the air.
  - (a) Is the velocity changing before it is at its highest point? (**YES**, ~~NO~~)
  - (b) Is the velocity changing after it is at its highest point? (**YES**, ~~NO~~)
  - (c) Is the velocity changing at its highest point? (**YES**, ~~NO~~)
  - (d) Is the object accelerating at its highest point? (**YES**, ~~NO~~).
5. You stand on a table and throw a ball up at a speed of 10.0 m/s. Your friend is lying on the floor and catches the ball. Just before your friend catches the ball, the ball is moving (~~THE SAME SPEED~~, **FASTER THAN**, ~~SLOWER THAN~~) you threw it.

# Free fall

## Problems

$$\begin{aligned} \textcircled{1} \text{ (a)} \quad v_i &= 6.0 \text{ m/s} \\ a &= -9.8 \text{ m/s}^2 \\ d &= 0 \\ t &= ? \end{aligned}$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$\begin{aligned} t &= \frac{-2v_i}{a} \\ &= \frac{-2(6.0)}{-9.8} \end{aligned}$$

$$\underline{t = 1.2 \text{ s}}$$

$$\begin{aligned} \text{(b)} \quad v_i &= 6.0 \text{ m/s} \\ a &= -9.8 \text{ m/s}^2 \\ v_f &= 0 \\ t &= ? \end{aligned}$$

$$v_f = v_i + at$$

$$\begin{aligned} t &= \frac{v_f - v_i}{a} \\ &= \frac{-6.0}{-9.8} \end{aligned}$$

$$\underline{t = 0.61 \text{ s}}$$

$$\begin{aligned} \textcircled{2} \text{ (a)} \quad v_i &= 0 \\ a &= -9.8 \text{ m/s}^2 \\ t &= 1.5 \text{ s} \\ d &= ? \end{aligned}$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$= \frac{1}{2} (-9.8) (1.5)^2$$

$$= -11.0 \text{ m}$$

∴ the bridge is 11.0 m high.

$$\begin{aligned} \text{(b)} \quad v_i &= 0 \\ a &= -9.8 \text{ m/s}^2 \\ t &= 1.5 \text{ s} \\ v_f &= ? \end{aligned}$$

$$\begin{aligned} v_f &= v_i + at \\ &= -9.8(1.5) \end{aligned}$$

$$= -14.7 \text{ m/s}$$

14.7 m/s downward.

$$\textcircled{3} \text{ (a) } v_i = 0$$

$$a = -1.62 \text{ m/s}^2$$

$$d = -0.95 \text{ m}$$

$$v_f = ?$$

$$v_f^2 = v_i^2 + 2ad$$

$$v_f = \sqrt{2(-1.62)(-0.95)}$$

$$v_f = 1.75 \text{ m/s}$$

1.75 m/s down.

$$\text{(b) } v_i = 0$$

$$a = -1.62 \text{ m/s}^2$$

$$d = -0.95 \text{ m}$$

$$t = ?$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$t = \sqrt{\frac{2d}{a}}$$

$$= \sqrt{\frac{2(-0.95)}{-1.62}}$$

$$\underline{t = 1.085}$$

$$\textcircled{4} \quad v_i = 30.0 \text{ m/s}$$

$$v_f = 0$$

$$a = -9.8 \text{ m/s}^2$$

$$d = ?$$

$$v_f^2 = v_i^2 + 2ad$$

$$d = \frac{v_f^2 - v_i^2}{2a}$$

$$= \frac{-(30)^2}{2(-9.8)}$$

$$\underline{d = 45.9 \text{ m}}$$

$$\begin{aligned} \textcircled{5} \quad v_i &= -100.0 \text{ m/s} \\ a &= -9.8 \text{ m/s}^2 \\ t &= 1.0 \text{ s} \\ v_f &= ? \end{aligned}$$

$$\begin{aligned} v_f &= v_i + at \\ &= -100 + (-9.8)(1) \\ &= -109.8 \text{ m/s} \\ &= \underline{109.8 \text{ m/s down}} \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad a &= -9.8 \text{ m/s}^2 \\ t &= 10.0 \text{ s} \\ d &= 0 \\ v_i &= ? \end{aligned}$$

$$\begin{aligned} d &= v_i t + \frac{1}{2} a t^2 \\ v_i &= -\frac{1}{2} a t \\ &= -\frac{1}{2} (-9.8)(10) \\ v_i &= \underline{49 \text{ m/s}} \end{aligned}$$

$$\begin{aligned} \textcircled{7} \quad \text{Ball A} \\ v_i &= 40 \text{ m/s} \\ a &= -9.8 \text{ m/s}^2 \\ d &= -20 \text{ m} \\ v_f &= ? \end{aligned}$$

$$v_f^2 = v_i^2 + 2ad$$

$$v_f = \sqrt{(40)^2 + 2(-9.8)(-20)}$$

$$v_f = 44.6 \text{ m/s down}$$

$$\begin{aligned} \text{Ball B} \\ v_i &= 0 \\ a &= -9.8 \text{ m/s}^2 \\ d &= -20 \text{ m} \\ v_f &= ? \end{aligned}$$

$$v_f^2 = v_i^2 + 2ad$$

$$v_f = \sqrt{2(-9.8)(-20)}$$

$$v_f = 19.8 \text{ m/s down}$$

$$\begin{aligned} \text{Ball C} \\ v_i &= -20 \text{ m/s} \\ a &= -9.8 \text{ m/s}^2 \\ d &= -20 \text{ m} \\ v_f &= ? \end{aligned}$$

$$v_f^2 = v_i^2 + 2ad$$

$$v_f = \sqrt{(-20)^2 + 2(-9.8)(-20)}$$

$$v_f = 28.1 \text{ m/s down}$$

Ball A is traveling fastest

$$\textcircled{8} \text{ (c)} \quad v_i = 20 \text{ m/s}$$

$$v_f = 10 \text{ m/s}$$

$$a = -9.8 \text{ m/s}^2$$

$$t = ?$$

$$v_f = v_i + at$$

$$t = \frac{v_f - v_i}{a}$$

$$= \frac{10 - 20}{-9.8}$$

$$t = \underline{1.02 \text{ s}}$$

$$\text{(b)} \quad v_i = 20 \text{ m/s}$$

$$v_f = -10 \text{ m/s}$$

$$a = -9.8 \text{ m/s}^2$$

$$t = ?$$

$$v_f = v_i + at$$

$$t = \frac{v_f - v_i}{a}$$

$$= \frac{-10 - 20}{-9.8}$$

$$t = \underline{3.06 \text{ s}}$$

$$\textcircled{9} \text{ (a)} \quad a = -9.8 \text{ m/s}^2$$

$$d = -50 \text{ m}$$

$$t = 5 \text{ s}$$

$$v_i = ?$$

$$d = v_i t + \frac{1}{2} at^2$$

$$v_i = \frac{d - \frac{1}{2} at^2}{t}$$

$$= \frac{-50 - \frac{1}{2}(-9.8)(5)^2}{5}$$

$$\underline{v_i = 14.5 \text{ m/s (up)}}$$

$$9(b) \quad v_f = 0$$

$$a = -9.8 \text{ m/s}^2$$

$$v_i = 14.5 \text{ m/s}$$

$$d = ?$$

$$v_f^2 = v_i^2 + 2ad$$

$$d = \frac{v_f^2 - v_i^2}{2a}$$

$$= \frac{-(14.5)^2}{2(-9.8)}$$

$$d = \underline{10.7 \text{ m}}$$

(10) throws

$$v_i = ?$$

$$a = -9.8 \text{ m/s}^2$$

$$t = 3.0 \text{ s}$$

$$d = \underline{-78.4 \text{ m}}$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$v_i = \frac{d - \frac{1}{2} a t^2}{t}$$

$$= \frac{-78.4 - \frac{1}{2}(-9.8)(3)^2}{3}$$

$$v_i = -11.4 \text{ m/s}$$

11.4 m/s down

drops

$$v_i = 0$$

$$a = -9.8 \text{ m/s}^2$$

$$t = 4.0 \text{ s}$$

$$d = ?$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$= \frac{1}{2}(-9.8)(4.0)^2$$

$$= -78.4 \text{ m}$$